

PHYS 215 - Mechanics I - Remake Quiz

2019-2020

Full Name:

KEY

Note: Each Question is 2 marks.

Question 1

A ball is horizontally thrown with a speed of 40 m/s as shown in the figure. The ball falls down in 3 seconds. (Take $g = -10 \text{ m/s}^2$)

A) Calculate the distance x .

B) Calculate the height, $h = ?$

$$\Delta y = h = v_{y0} t_{\text{fall}} + \frac{1}{2} g t_{\text{fall}}^2$$

$$\Delta y = h = 0 + \frac{1}{2} (-10) 3^2$$

$$h = -45 \text{ m}$$

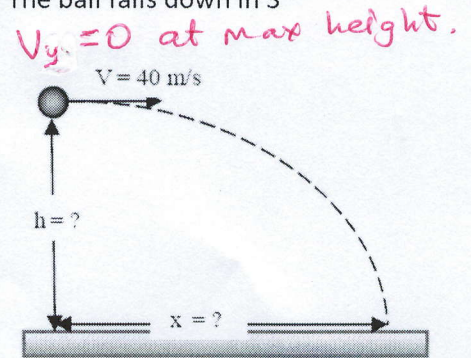
$$a) x = v_x \cdot t_{\text{fall}}$$

$$v_x = 40 \text{ m/s}$$

$$t_{\text{fall}} = 3 \text{ s}$$

$$= 40 \frac{\text{m}}{\text{s}} \cdot 3 \text{ s}$$

$$x = 120 \text{ m}$$

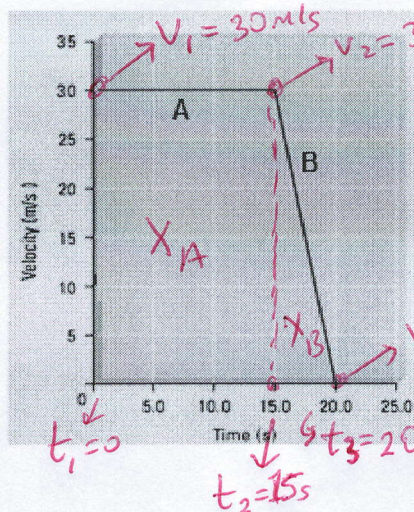


Question 2

The graph below shows the change in the velocity of a car with time.

A) Calculate the distance taken by the car for 20 seconds.

B) Calculate the acceleration of the car for a) 0 - 15 seconds and b) 15 - 20 seconds.



A) $x_A = 30 \times 15 = 450 \text{ m}$ $x_B = \frac{30 \cdot (20-15)}{2}$

The area under the v-t graph gives the distance taken.

$$x_B = \frac{30 \cdot 5}{2} = 75 \text{ m}$$

$$x_T = x_A + x_B = 450 + 75 = 525 \text{ m}$$

B) $a = \frac{\Delta v}{\Delta t} \Rightarrow a_A = \frac{v_2 - v_1}{t_2 - t_1} = \frac{30 - 30}{15 - 0} = 0 \text{ m/s}^2$ $a_B = \frac{v_3 - v_2}{t_3 - t_2} = \frac{0 - 30}{20 - 15} = \frac{-30}{5} = -6 \text{ m/s}^2$

Question 3

A ball thrown up with an initial velocity of 20 m/s.

A) How long does it take the ball to reach its maximum height?

B) What is the max height the ball reaches?



$$A) v_{yf} = v_{y0} + g t$$

$$v_{yf} = 0 = 20 + (-10) t$$

$$-20 = -10 t \Rightarrow t = \frac{-20}{-10} = 2 \text{ s}$$

$$t = 2 \text{ s}$$

$$B) \Delta y = h = v_{y0} t + \frac{1}{2} g t^2$$

$$= 20 \cdot 2 + \frac{1}{2} (-10) 2^2$$

$$= 40 - 20$$

$$\Delta y = 20 \text{ m}$$

Question 4

A car initially at rest starts to move with a constant acceleration of 4 m/s^2 . If it accelerates for 12 seconds,

- A) How far will it move during this time?
- B) What will be its final velocity?

$$V_{x0} = 0 \quad a = 4 \text{ m/s}^2 \quad t = 12 \text{ s}$$
$$A) \Delta x = V_{x0}t + \frac{1}{2}at^2 = \frac{1}{2}4(12)^2$$
$$\boxed{\Delta x = 288 \text{ m}}$$

$$B) V_{xf} = V_{x0} + at$$
$$\boxed{V_{xf} = 4 \cdot 12 = 48 \text{ m/s}}$$

Question 5

The position of a particle moving on an x axis is given by $x = 4t^2 - 6t + 10$

- A) Find the velocity of the particle at $t = 2 \text{ s}$
- B) Find the acceleration of the particle.

$$A) v = \frac{dx}{dt} = \frac{d(4t^2 - 6t + 10)}{dt}$$
$$v = 8t - 6 \Rightarrow \text{at } t = 2 \text{ s} \quad v = 8 \cdot 2 - 6$$
$$= 16 - 6$$
$$\boxed{v = 10 \text{ m/s}}$$

$$B) a = \frac{dv}{dt} = \frac{d(8t - 6)}{dt} = 8$$
$$\boxed{a = 8 \text{ m/s}^2}$$

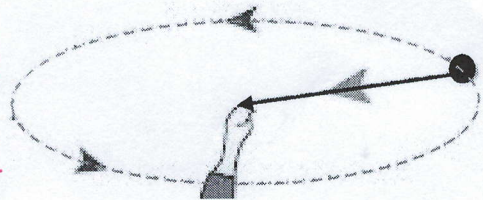
Question 6

A ball rotates at a constant speed of 2 m/s at the end of 2 m long string. The string makes a horizontal circle.

- A) Calculate the centripetal acceleration of the ball
- B) Calculate the period of the motion.

$$A) a_c = \frac{v^2}{R}$$
$$\boxed{a_c = \frac{2^2}{2} = 2 \text{ m/s}^2}$$

$$B) T = ? \quad v = \frac{x}{T} \Rightarrow T = \frac{x}{v} = \frac{2\pi r}{v}$$
$$T = \frac{2 \cdot (3.14) \cdot 2}{2} = 6.28 \text{ s}$$



Question 7

The position vector for a particle is initially $\vec{r}_i = (-4.0 \text{ m})\hat{i} - (1.0 \text{ m})\hat{j} + (2.0 \text{ m})\hat{k}$

and then later is $\vec{r}_f = (3.0 \text{ m})\hat{i} - (1.0 \text{ m})\hat{j} + (3.0 \text{ m})\hat{k}$

What is the particle's displacement \vec{r} from \vec{r}_i to \vec{r}_f ?

$$\Delta \vec{r} = \vec{r}_f - \vec{r}_i = (x_f - x_i)\hat{i} + (y_f - y_i)\hat{j} + (z_f - z_i)\hat{k}$$
$$= (3 - (-4))\hat{i} + (-1 - (-1))\hat{j} + (3 - 2)\hat{k}$$
$$= 7\hat{i} + 0\hat{j} + 1\hat{k}$$
$$\boxed{\Delta \vec{r} = 7\hat{i} + \hat{k}}$$